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## Aluminium anodising in low acidity sulphate baths: growth mechanism and nanostructure of porous anodic films

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**Abstract** Overall kinetic and chronopotentiometric studies were performed during Al anodising in H<sub>2</sub>SO<sub>4</sub>, 0–5% w/v, bath solutions pure and saturated by Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>. Peculiarities in film growth mechanism and nanostructure in these cases appeared, like significant differences of porosity and its dependence on film thickness, different critical current density above which pitting appears, salt deposition on pitted surface regions in saturated bath, etc. The different conditions inside pores are responsible for this behaviour like almost depletion of H<sup>+</sup> during a long initial transient stage in the first case, supersaturation and formation of Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> nanoparticle micelles on pore surface in the second case, etc. Differences in film growth mechanism also appeared between these and alike baths at higher acidity. Anodising in low acidity saturated baths shows superiority for growing low porosity films at specific conditions. New technologies may be suggested to produce optimal films of desired structure.

**Keywords** Porous anodic aluminas · Low acidity sulphate baths · Chronopotentiometry and overall kinetics · Growth mechanism and nanostructure · Interface colloidal Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>

### Nomenclature

$a_{H^+, 0}$  Activity of H<sup>+</sup> in the bath bulk solution  
 $a_{H^+, x}$  Activity of H<sup>+</sup> in the pore filling solution at distance  $x$  from the film surface  
 $a_{H^+, b}$  Activity of H<sup>+</sup> in the pore filling solution at pore bases  
 $A$  Dimensionless factor equal to  $(kjt - m)(4^{-1}\pi S_g d_c k' t)^{-1}$

$A_0$   $nD_b^2$   
 $A_1$  and  $A_2$  Parameters derived by fitting the equation  $A = A_0 + A_1 t + A_2 t^2$  to the experimental results  $A$  versus  $t$   
 $A'_1$  and  $A'_2$  Parameters derived by fitting the equation  $A = A_0 + A_1 h + A_2 h^2$  to the experimental results  $A$  versus  $h$   
**B** Appearance of burning regions on the surface, i.e. advanced, dark colour, black pitting  
 $C_{a,0}$  Concentration of H<sub>2</sub>SO<sub>4</sub> in the bath bulk solution  
 $C'_{a,0}$  Concentration of H<sub>2</sub>SO<sub>4</sub> in the bath bulk solution just exceeding 5% w/v where the  $j_c$  becomes identical for both solutions of pure H<sub>2</sub>SO<sub>4</sub> and saturated by Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>  
 $C_{a,x}$  Concentration of H<sub>2</sub>SO<sub>4</sub> in the pore filling solution at distance  $x$  from the film surface  
 $C_{a,b}$  Concentration of H<sub>2</sub>SO<sub>4</sub> at pore bases  
 $C_{H^+,0}$  Concentration of H<sup>+</sup> in the bath bulk solution  
 $C_{H^+,x}$  Concentration of H<sup>+</sup> in the pore filling solution at distance  $x$  from the film surface  
 $C_{H^+,b}$  Concentration of H<sup>+</sup> at pore bases  
 $C_{s,0}$  Concentration of Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> in the bath bulk solution  
 $C_{s,x}$  Concentration of Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> in the pore filling solution at distance  $x$  from the film surface  
 $C_{s,b}$  Concentration of Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> at pore bases  
 $C_{s,s}$  Saturation concentration of Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> in the bath bulk solution  
**d.** Dense H<sub>2</sub>SO<sub>4</sub> (95–97% w/w)  
 $d_c$  Density of the compact pore wall oxide, 3.42 g cm<sup>-3</sup>  
 $D_b$  Pore base diameter  
 $D_x$  Pore diameter at distance  $x$  from the film surface  
 $D_c$  Cell width

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$\Delta V$	Anodising voltage
$\Delta V'_m$	Minimum value of $\Delta V$ attained after the initial short transient stage in a time of the order of 1 min
$\Delta V_m$	Minimum value of $\Delta V$ attained within the quasi-steady state stage of film growth in saturated baths in a time of the order of ten or of some tens min
$h$	Film thickness
$j$	Current density
$j_c$	Critical current density above which pitting appears
$k$	Constant for oxide production resulting from Faraday's law
$k''$	Constant, $3.09 \times 10^{-6} \text{ cm}^3 \text{ mA}^{-1} \text{ min}^{-1}$
$k'$	$k''j$
$m$	Mass of oxide spread over the whole anodised geometric surface area of Al specimens
$n$	Surface density of pores
$p$	Porosity $v/v$
$\text{pH}_{\text{in}}$	pH of solution before anodising
$\text{pH}_{\text{fin}}$	pH of solution after each anodising run in each separate condition at one or different anodising times
P	Appearance of pitting regions on the surface
$r_x$	Rate of pore wall oxide dissolution reaction at distance $x$ from the film surface
S	Development of salt deposit layer on the pitted or burnt surface regions
$S_g$	Geometric surface area of Al specimens, $30.75 \text{ cm}^2$
$T$	Bath temperature
$T_x$	Temperature inside the pores at distance $x$ from the film surface
$T_b$	Temperature inside the pores around their bases
$t$	Time of anodising
$t_1$	Time up to which film thickness increases linearly with time
$t_m$	Time at which the maximum pore diameter near or at film surface approaches first the cell width that is $t_m \leq t_1$
$t_c$	Time at which a quasi-steady state maximum limiting $h$ or $m$ is first established

## Introduction

The porous anodic alumina films are important materials applied to improve the mechanical properties of Al [1], as anti-corrosion [2–4] and decorating [2, 3] coatings and membranes [5], in magnetic memories [6], catalysis [7–13], nuclear reactors [14], re-chargeable batteries [15], as templates for synthesising emitters [16, 17], etc. Due to their nanometer scale porous structure [2, 3, 7–13] and

sizes of particles constituting the pore wall material [18] recently, they have found application in nanoscience and nanotechnology, e.g. forms for electroplating metal nanowires [19–21], templates for creating C [22, 23] or TiO<sub>2</sub> [24, 25] nanotubes, nanoparticle sized ultra active catalysts or supports [11–13], etc. Their optimal effectiveness depends on their suitably designed, porous structure, nature/composition of pore wall oxide and reactive properties. These films are formed in phosphoric, oxalic, chromic, and sulphuric acid solutions [2, 3, 26, 27]. Also, bisulphates [28, 29] and mixtures of H<sub>2</sub>SO<sub>4</sub> with sulphate salts were used [28, 30–35]. H<sub>2</sub>SO<sub>4</sub> has been employed most frequently. The structure of uniformly/regularly grown films is defined by the surface density of pores, diameter at their bases and real shape of pores.

The films formed in H<sub>2</sub>SO<sub>4</sub> have a surface pore density of the order  $10^{10}$  or  $10^{11} \text{ cm}^{-2}$  [12, 30], depending solely on, and reduced with, current density [30, 36]. The pore base diameter varies from several nm to a few ten nm [30] depending on, and increasing with, temperature and H<sup>+</sup> activity at pore bases [28, 29]. The pores generally open towards the surface due to chemical dissolution of pore walls by the electrolyte during anodising [2, 37–41], similar to open circuit dissolution [37–41]. It is a first order reaction with respect to H<sup>+</sup> activity and is hindered by incorporated electrolyte anions [28]. At prolonged anodising due to pore opening [42, 43] a quasi-maximum limiting thickness may appear [2, 3, 42] decreasing with pore density, temperature and H<sup>+</sup> activity.

Conditions like low temperatures and electrolyte concentrations and high current densities in which, in addition, condensed Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> is not formed inside pores, favour the growth of low porosity hard films [2, 3]. Sulphate additives like Na<sub>2</sub>SO<sub>4</sub>, Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>, MgSO<sub>4</sub>, MnSO<sub>4</sub>, (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> and NiSO<sub>4</sub> [30–34] were believed to reduce the solvent action of electrolyte, thus favouring hard films. But, actually, their presence may increase the H<sup>+</sup> activity and always increases the concentration of incorporated anions [28, 29, 35]; the first may increase the pore base diameter and rate of pore wall dissolution reaction but the second reduces that rate. Its reduction can prevail in some cases. Conditions as above [43–45] and additives like Na<sub>2</sub>SO<sub>4</sub> [30], Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> and MgSO<sub>4</sub> [31], etc. also favour pitting appearance due to non-uniform/abnormal growth of films which excessively thicken locally [43–45]. Non-uniform aspect, thickness, porous structure, porosity, hardness and roughness and cracks appear. Hard films and pitting are together favoured [44, 45]. Though hard films with specific structural features seem to be formed in low acidity pure H<sub>2</sub>SO<sub>4</sub> baths, against expectations, relevant practices are absent.

Condensed Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> appears as colloidal Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub> nanoparticle micelles on the surface of pores [35]. The field at pore base and solid surface of pores catalyse their formation. They appear and disappear according to a quasi-equilibrium process and affect the kinetics and mechanism of film growth by reducing the surface fraction of charge exchange and diameter at pore bases

and the real fraction of wall surface where oxide dissolves; the mechanism of regular film growth is also enhanced. Their coagulation is prevented by their similar charge. Saturated  $\text{H}_2\text{SO}_4 + \text{Al}_2(\text{SO}_4)_3$  baths exert maximal such effects. The study of Al anodising in saturated baths  $\text{H}_2\text{SO}_4$  15–105% w/v [46] revealed many details of critical role of micelles and conditions inside pores.

The solubility of  $\text{Al}_2(\text{SO}_4)_3$  decreases with  $\text{H}_2\text{SO}_4$  concentration up to 95% w/v [35]. Saturated low acidity baths must have  $\text{Al}^{3+}$  and  $\text{SO}_4^{2-}$  concentrations close to the highest possible ones. The research of Al anodising in low acidity baths appears interesting especially that concerning: (1) the mechanism of film growth in low acidity  $\text{H}_2\text{SO}_4$  solutions either pure or saturated; (2) the comparison of growth mechanisms and structural features of films to explain the heretofore non use of low acidity baths; (3) predictions to optimise the process as regards the conditions of regular film growth and certain structural features at low acidity. This is the new idea of this study. A combined overall kinetic/chronopotentiometric method was applied that can effectively discover this mechanism since other methods applied i.e. to barrier type films are ineffective, inaccurate or inapplicable due to the existence of pores [28, 35, 46].

## Experimental

For preparing the anodising solutions  $\text{H}_2\text{SO}_4$ , 95–97% w/w (Merck, pro analysi), and  $\text{Al}_2(\text{SO}_4)_3 \cdot 18\text{H}_2\text{O}$  (Merck, extra pure, purity  $\geq 99.5777\%$ , 2% aqueous solution of which has a  $\text{pH} \approx 2.5\text{--}4.0$ ) reagents were used. The solubility of  $\text{Al}_2(\text{SO}_4)_3$  in  $\text{H}_2\text{SO}_4$  solutions at  $\text{H}_2\text{SO}_4$  concentrations 0 and 5% w/v ( $0.51 \text{ mol dm}^{-3}$ ) at  $25^\circ\text{C}$  was first determined as previously [35] described; it was  $\approx 1.05$  and  $0.98 \text{ mol dm}^{-3}$ , respectively. The anodic oxidation of Al was performed galvanostatically in thermostated and vigorously agitated saturated  $1 \text{ dm}^3$   $\text{Al}_2(\text{SO}_4)_3$  solution as well as in that solution acidified by dense  $\text{H}_2\text{SO}_4$ , 95–97% w/w, to  $\text{H}_2\text{SO}_4$  concentration  $\approx 1.55\%$  w/v. The anodising conditions were temperature  $25^\circ\text{C}$ , current density  $15 \text{ mA cm}^{-2}$  and time 15 min which in cases of pitting growth is sufficient for its development and easy detection [43, 44]. Though the  $\text{Al}_2(\text{SO}_4)_3$  solubility decreased with  $\text{H}_2\text{SO}_4$  concentration, to assure saturated bath irrespective of any slight change of its composition and temperature in subsequent experiments, a small amount of  $\text{Al}_2(\text{SO}_4)_3$  was added, 0.05 mol, which did not change appreciably the volume of solution; the  $\text{Al}_2(\text{SO}_4)_3$  content, thus, reached  $\approx 1.1 \text{ mol dm}^{-3}$ . The acidification and anodising in the above conditions continued at different steps up to  $\text{H}_2\text{SO}_4$  concentration  $\approx 3\%$  w/v. Finally, a current density of  $35 \text{ mA cm}^{-2}$  was also employed. The method of acidification with small amounts of dense  $\text{H}_2\text{SO}_4$ , 95–97% w/w, was adopted to: (1) obtain desired  $\text{H}_2\text{SO}_4$  concentrations or pH's; (2) bypass difficulties in determining  $\text{Al}_2(\text{SO}_4)_3$  solubility in  $\text{H}_2\text{SO}_4$  solutions of low concentrations, between 0 and

5% w/v since it must vary imperceptibly; (3) easily prepare saturated solutions at low  $\text{H}_2\text{SO}_4$  concentrations.

Anodic oxidation of Al was also performed in saturated  $\text{H}_2\text{SO}_4$   $0.51 \text{ mol dm}^{-3} + \text{Al}_2(\text{SO}_4)_3$   $0.98 \text{ mol dm}^{-3}$  solution at the above temperature and current densities and different times up to 140 min and in pure  $\text{H}_2\text{SO}_4$  solutions 1, 2 and 3% w/v at 15 min and 5% w/v at different times up to 160 min.

The added  $\text{Al}_2(\text{SO}_4)_3$  in amounts 1.05 or  $1.1 \text{ mol dm}^{-3}$  for saturated solutions of  $\text{H}_2\text{SO}_4$  up to 3% w/v and  $0.98 \text{ mol dm}^{-3}$  at 5% w/v, was slightly higher than the saturation one. The small amount of precipitate could not appreciably hinder stirring of bath but, in turn, it always assured saturated solution. The pH of solutions at  $25^\circ\text{C}$  was measured before and after each anodising run in each separate condition at one or different anodising times.

Al sheets 0.5-mm thick and 99.5% pure were used. The composition of Al, shape and dimensions of Al anodes and Pb cathodes used and the procedure for washing and neutralizing Al specimens after anodising to remove  $\text{H}_2\text{SO}_4$  and  $\text{Al}_2(\text{SO}_4)_3$  from the pores and their drying were described earlier [35, 42].

The anodising of Al was also followed chronopotentiometrically. During galvanostatic anodising in saturated baths and film thickening, after some time interval from the start characterised by certain details (see later), the anodic potential required to keep constant current always increases [35]. As verified this potential, determined as previously [47], which almost coincides with the potential drop from the double layer at pore bases to the oxide | metal interface [28, 35], is close to the anodising voltage. For convenience, the latter was recorded. The required voltage increase, also met here, continued up to  $\approx 50 \text{ V}$ ; then, anodising was interrupted.

The masses of films, necessary for the overall kinetic study, were determined as previously [43]. All anodised Al specimens were examined macroscopically and microscopically to verify the growth or not of pitting or burning (advanced, dark colour, black pitting) as described earlier [44] and occurrence of other phenomena.

## Results

General observations for the anodising process, related phenomena and film morphology

The results appear in Table 1. The successive lines represent steps of experiments and observations. The numbers in parentheses show the bath obtained after the step corresponding to this number; d means dense  $\text{H}_2\text{SO}_4$  (95–97% w/w);  $\text{pH}_{\text{in}}$  and  $\text{pH}_{\text{fi}}$  are the pH's before and after anodising;  $j$  is the current density;  $t$  is the time of anodising at temperature ( $T$ ) =  $25^\circ\text{C}$ ;  $C_{\text{a},0}$  is the (estimated)  $\text{H}_2\text{SO}_4$  concentration, P and B mean the appearance of pitted or burnt surface regions and S means the development of an  $\text{Al}_2(\text{SO}_4)_3$  salt deposit

**Table 1** Conditions of anodic oxidation of Al and observations concerning the appearance of pitting, P, burning, B, and salt deposition on the pitted and burnt regions of specimens, S, in both saturated and pure acid solutions

Number of experimental step	Bath composition	pH <sub>in</sub>	$j/\text{mA cm}^{-2}$	$t/\text{min}$	pH <sub>f</sub>	Estimated $C_{a,0}$ , % w/v	Appearance of P, B and S
1	$\text{Al}_2(\text{SO}_4)_3$ 1.05 mol dm <sup>-3</sup>	2.331	15	15	2.387	0	Macroscopic P and B, S
2	(1) + 8.1 ml d. $\text{H}_2\text{SO}_4$ per dm <sup>3</sup> of solution	1.180	15	15	1.189	1.55	Macroscopic P and B, S
3	(2) + 0.05 mol $\text{Al}_2(\text{SO}_4)_3$ per dm <sup>3</sup> of solution (total 1.1 mol dm <sup>-3</sup> $\text{Al}_2(\text{SO}_4)_3$ )	1.245	–	–	1.245	1.55	–
4	(3) + 3.8 ml d. $\text{H}_2\text{SO}_4$ per dm <sup>3</sup> of solution	0.708	15	15	0.699	2.10	Macroscopic P and B, S
5	(4) + 1.4 ml d. $\text{H}_2\text{SO}_4$ per dm <sup>3</sup> of solution	0.601	15	15	0.595	2.35	Macroscopic P and B, S
6	(5) + 3.5 ml d. $\text{H}_2\text{SO}_4$ per dm <sup>3</sup> of solution	0.411	15	15	0.410	2.97 ≈ 3	Macroscopic P or B, S
7	(6)	0.410	35	15	0.412	2.97 ≈ 3	Very intense macroscopically observed P and B, S
8	$\text{Al}_2(\text{SO}_4)_3$ 0.98 mol dm <sup>-3</sup> + $\text{H}_2\text{SO}_4$ 0.51 mol dm <sup>-3</sup>	0.043	15	Various $t$ 's ≤ 140 min	0.062	5.0	Microscopically well observed and macroscopically just observed P
9	(8)	0.062	35	Various $t$ 's ≤ 54.45 min	0.081	5.0	Macroscopically observed P, small area S.
10	$\text{H}_2\text{SO}_4$ 0.102 mol dm <sup>-3</sup>	1.180	15	15	1.190	1.0	Macroscopic P and B
11	$\text{H}_2\text{SO}_4$ 0.204 mol dm <sup>-3</sup>	0.753	15	15	0.758	2.0	Macroscopic P and B
12	$\text{H}_2\text{SO}_4$ 0.306 mol dm <sup>-3</sup>	0.601	15	15	0.602	3.0	Macroscopic P and B
13	$\text{H}_2\text{SO}_4$ 0.51 mol dm <sup>-3</sup>	0.411	15	Various $t$ 's ≤ 160 min	0.435	5.0	Microscopically observed P
14	$\text{H}_2\text{SO}_4$ 0.51 mol dm <sup>-3</sup>	0.435	35	15	0.439	5.0	Macroscopic P and B

layer on the pitted or burnt regions. The noted  $\text{Al}_2(\text{SO}_4)_3$  concentration ( $C_{s,0}$ ) almost equals, actually it is imperceptibly higher than, the saturation one ( $C_{s,s}$ ). The citation of photographs/microphotographs of pitted surfaces for all  $C_{a,0}$ 's employed is unnecessary as they were similar to those given earlier [43, 44], adding no new information.

The following observations derived from Table 1 and additional ones were made.

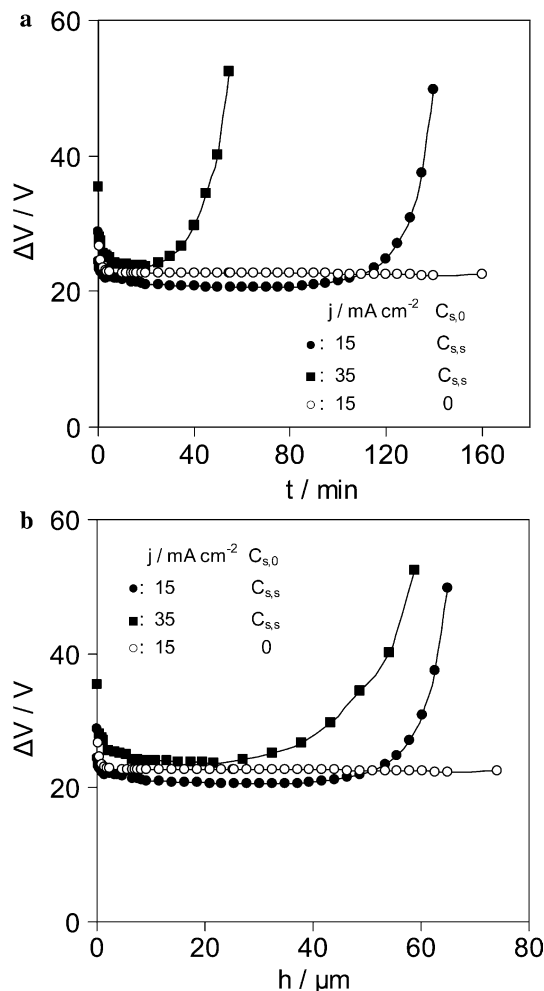
1. The addition of acidifying  $\text{H}_2\text{SO}_4$  up to pH's 1.180, 0.601 and 0.411 (i.e. the pH's of pure  $\text{H}_2\text{SO}_4$  1, 3 and 5% w/v solutions) yielded  $\text{H}_2\text{SO}_4$  concentrations different than the corresponding ones in pure acid solutions; the presence of salt alters the acidity of solution, apparently due to its acidic character, the lower enough real  $\text{H}_2\text{O}$  concentration and the effect of salt on the equilibrium processes.
2. The anodising process does not affect appreciably the pH and  $C_{a,0}$  of solution during a few experiments.
3. The solution of  $\text{Al}_2(\text{SO}_4)_3$  alone, without adding  $\text{H}_2\text{SO}_4$ , is acidic and anodic oxidation of Al well takes place in this solution; nevertheless, it is accompanied with the development of strong pitting in the form of P and B.
4. At  $C_{s,0} = C_{s,s}$  and  $C_{a,0} = 0$ –5% w/v pitting appears. At identical  $j$ 's and  $t$ 's (or mean film thicknesses) pitting

weakened with  $C_{a,0}$  and at  $C_{a,0} = 5\%$  w/v it was just detected at the lower  $j$  occupying negligible surface area, estimated to be <1%. At identical  $t$ , pitting in steps 7 and 9 was much stronger than in 6 and 8; thus the rise of  $j$  reinforces growth of pitting. It became stronger with  $t$ , at least for  $C_{a,0} \leq 3\%$  w/v where it was clearly observed.

5. At  $C_{s,0} = 0$  and  $C_{a,0} \leq 5\%$  w/v pitting also appeared reinforced with increasing  $t$  and  $j$  and decreasing  $C_{a,0}$ ; at  $j = 15 \text{ mA cm}^{-2}$  and  $C_{a,0} = 5\%$  w/v it was just microscopically detected. The results at  $C_{s,0} = 0$  and  $C_{s,0} = C_{s,s}$  and constant either pH or  $C_{a,0}$  and  $t$  showed that the addition of  $\text{Al}_2(\text{SO}_4)_3$  at  $C_{s,0} = C_{s,s}$  reinforces pitting, unlike the case  $C_{a,0} \geq 15\%$  w/v [35, 46]. The differences decayed with  $C_{a,0}$  and at  $C_{a,0} = 5\%$  they became inappreciable.
6. Condensed  $\text{Al}_2(\text{SO}_4)_3$  salt deposit, like fractals, appeared just above the P or B regions, clearly observed after anodising, that was removed during the washing of specimens. This is consistent with the higher rates of anodic oxidation of Al and production of  $\text{Al}_2(\text{SO}_4)_3$  in the pitted surface, which is smaller than the rest [44], due to the “field assisted” pore base oxide dissolution [2, 3, 30, 32–34, 48–50] and pure chemical wall dissolution [2, 37–41].

## Chronopotentiometric study

The plots of required anodising voltage ( $\Delta V$ ) versus  $t$  at  $C_{a,0}=5\%$  w/v,  $C_{s,0}=0$  and  $C_{s,0}=C_{s,s}$  are given in Fig. 1a. The  $\Delta V$  increased abruptly up to a high value depending on  $C_{a,0}$  and  $j$  in a time of the order of 1 s that marks the nucleation of pores. During a next short transient stage of the order of 1 min it decreased up to a time  $t(\Delta V'_m)$  at which  $\Delta V$  becomes minimum ( $\Delta V'_m$ ). In this stage, a quasi-steady state pore base diameter, nature/composition of barrier layer and electrolyte composition inside the pores are established. After the initial transient at  $C_{s,0}=0$  the  $\Delta V$  on average decreases slightly (or remains almost constant) with  $t$  while at  $C_{s,0}=C_{s,s}$  a minimum,  $\Delta V_m$ , appears at  $t=t(\Delta V_m) > t(\Delta V'_m)$  of the order of ten or of several ten min and at  $t > t(\Delta V_m)$  it increases initially slightly and later strongly. At the other  $C_{a,0}$ 's  $\Delta V$  varied with  $t$  up to the  $t$ 's employed similarly as above; it also increased with  $j$  and decreased with  $C_{a,0}$



**Fig. 1** Variation of the anodising voltage,  $\Delta V$ , with time,  $t$ , (a) and film thickness,  $h$ , (b) at  $H_2SO_4$  concentration  $C_{a,0} = 5\%$  w/v, current densities  $j = 15$  and  $35$  mA cm<sup>-2</sup> and in saturated  $H_2SO_4$  solution,  $C_{s,0} = C_{s,s}$ , and pure  $H_2SO_4$  solution,  $C_{s,0} = 0$

in both cases. At  $C_{a,0}$ 's  $\leq 3\%$  w/v in both cases pitting was strong enough, the mechanism of film growth deviates strongly from that of regular one and the  $t$  employed was relatively small; thus, citation of relevant chronopotentiometric curves was judged unnecessary as it added no new information. But at  $C_{a,0} = 5\%$  w/v pitting was weak enough and comparable in both cases; the mechanism of film growth approaches that of regular one and their citation yields much important information (see later).

The thickness of uniformly/regularly grown films or the average one of irregular films ( $h$ ) is given by

$$h = k't = k''jt, (t \leq t_1), \quad (1)$$

where  $k''$  is a constant  $3.09 \times 10^{-6}$  cm<sup>3</sup> mA<sup>-1</sup> min<sup>-1</sup> and  $t_1$  is the time up to which  $h$  increases linearly with  $t$  [42]. The  $t_1$  is identical to, or slightly higher than,  $t_m$  that is the time at which the maximum average diameter of pores at a position along them, usually at or near film surface, approaches first the cell width ( $D_c$ ). At  $t_m$  the surface appearance starts to change from a shiny, transparent and similar to Al metal to a mat, milky one [42–44]. For  $t > t_1$   $h$  increases with retarded rate with  $t$  up to a  $t = t_c$  where it may become  $\approx 0$ ; then a quasi-maximum limiting  $h$  may be achieved exceeding slightly or appreciably  $k''jt_m$  or  $k''jt_1$  [42, 43]. All  $t$ 's employed at  $C_{a,0} = 5\%$  w/v were  $< t_m$  for the much larger non-pitted surface region; probably this is valid also for the pitted regions since at this  $C_{a,0}$  pitting is slight and the rate of  $h$  increase does not notably differ from that in the rest surface. Using Eq. 1,  $\Delta V$  versus  $h$  [ $h \leq h(t_m)$ ] plots were constructed, Fig. 1b, which differ in their relative positions from those in Fig. 1a.

## Overall kinetic study

For the noted reasons, the kinetics of film growth at  $C_{a,0} = 5\%$  w/v has a specific significance in relation to the other  $C_{a,0}$ 's. The plots of film mass ( $m$ ) spread over the entire anodised geometric surface of Al specimens ( $S_g = 30.75$  cm<sup>2</sup> [42]) versus  $t$  are given in Fig. 2a. The  $m$  versus  $h$  [ $h \leq h(t_m)$ ] plots are given in Fig. 2b.

At  $C_{s,0} = 0$  and constant  $j$ , when the film growth is regular and the pore base diameter ( $D_b$ ) remains constant during anodising, met when  $Al_2(SO_4)_3$  colloidal micelles are not formed at pore base [35], the  $\Delta V$  versus  $t$  plot shows an almost horizontal plateau for  $t > t(\Delta V'_m)$ . Then, the kinetic model

$$A = (kjt - m)(4^{-1}\pi S_g d_c k't)^{-1} = A_0 + A_1 t + A_2 t^2 \\ = 4\pi^{-1}p, [A_0, A_1, A_2 > 0 \text{ and } t(\Delta V'_m) \leq t \leq t_m] \quad (2)$$

applies irrespective of pore shape [42, 43], where  $A$  is a dimensionless factor;  $k$  is a constant resulting from Faraday's law;  $d_c$  is the density of compact pore wall oxide ( $3.42$  g cm<sup>-3</sup>) [42];  $A_0 = n D_b^2$ , where  $n$  is the surface pore density;  $A_1$  and  $A_2$  are parameters depending on  $j$  and  $T$  and  $p$  is porosity (v/v). The physical meaning

of  $A$  is derived from its relation with  $p$  that depends on the structural features  $n$  and  $D_b$  and geometry of pores defined by the process of pore wall dissolution along the pores. The  $A_1$  and  $A_2$  are derived on the basis of complex kinetics of this process and embrace kinetic and geometric parameters [36, 43]. From Eqs. 1 and 2

$$A = A_0 + A_1 h + A_2 h^2 \\ = 4^{-1} \pi p, [A_0, A_1, A_2 > 0 \text{ and } h[t(\Delta V'_m)] \leq h \leq h(t_m)]. \quad (3)$$

For  $t=0$  the model (2) gives  $A_0 = 4\pi^{-1} p$  but initially only a barrier layer exists with zero  $p$ . Thus, it applies after the  $t$  of pore nucleation, which is of the order of 1 s [28], i.e. negligible compared to  $t$ 's employed. The limitation  $t(\Delta V'_m) \leq t \leq t_m$  always satisfies this condition. The  $A$  (or  $p$ ) is related to basic features like  $n$ ,  $D_b$ , etc. and magnifies the  $m$  differences permitting detailed/accurate studies of regular film growth [28, 36, 43].

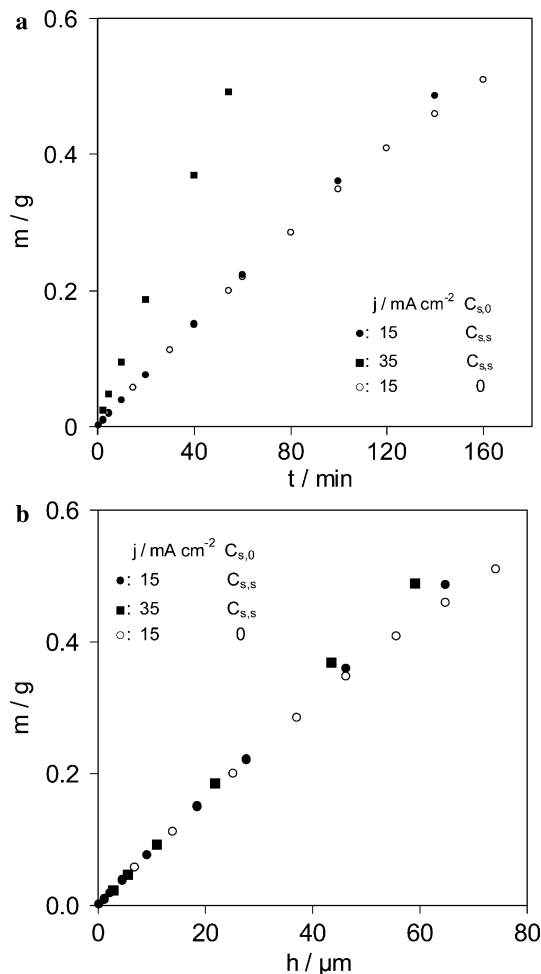
When at high  $C_{a,0} \geq 15\%$  w/v and  $t > t(\Delta V'_m)$   $\Delta V$  rises significantly with  $t$ , a scatter of points is usually

observed and the  $A$  versus  $t [t(\Delta V'_m) \leq t \leq t_m]$  and  $h [h[t(\Delta V'_m)] \leq h \leq h(t_m)]$  plots at  $C_{s,0} = C_{s,s}$  obey the equation

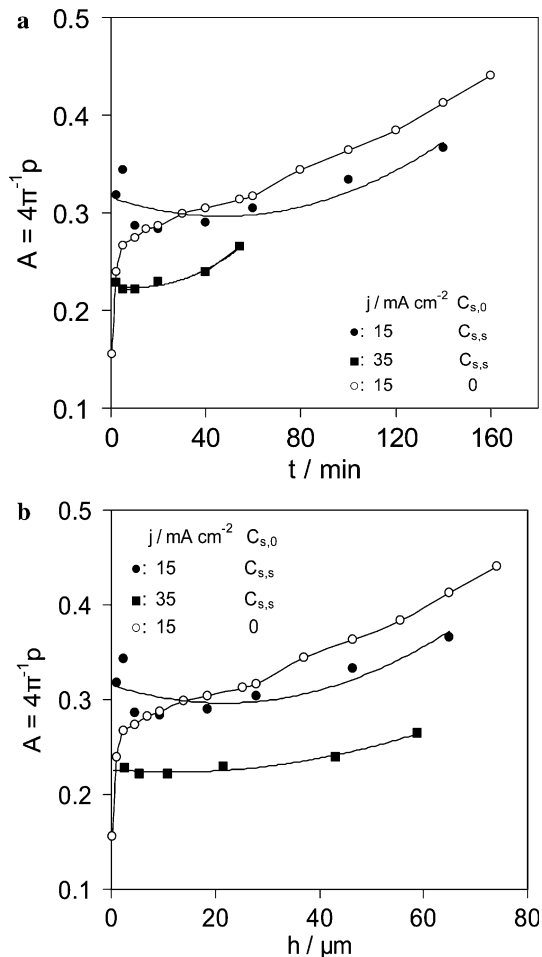
$$A \approx A_0 + A_1 t + A_2 t^2 = A_0 + A'_1 h + A'_2 h^2 \quad (4)$$

where  $A_0$ ,  $A_2$  and  $A'_2$  are  $>0$  while  $A_1$  and  $A'_1$  are usually  $>0$  at low  $j$ 's and gradually become  $<0$  at higher  $j$ 's and minima appear [35]. Irrespective of pitting appearance or not, colloidal  $\text{Al}_2(\text{SO}_4)_3$  nanoparticle micelles form at least on the pore base surface affecting the mechanism of film growth. The average  $D_b$  decreases with  $t$  or  $h$  [35]. As  $A_1$  (or  $A'_1$ ) becomes lower,  $D_b$  decreases faster with  $t$  or  $h$  and/or the average rate of chemical pore wall dissolution decreases, both due mainly to the increase of surface fraction occupied by micelles. Only in this case reduction of  $p$  with  $t$  or  $h$  can be observed. Also in this case  $A_0 = nD_b^2$ , where now  $D_b$  is the steady state one for  $t \rightarrow 0$  and  $A_1$  and  $A_2$  additionally embrace the deviation of  $D_b$ 's at  $t > 0$  from the above steady state one.

The  $A$  versus  $t$  and  $h$  plots are given in Fig. 3a and b. Figures 1 and 3 show that at  $C_{s,0} = 0$  the  $A$  versus  $t$  and  $h$



**Fig. 2** Variation of the film mass,  $m$ , with time,  $t$ , (a) and film thickness,  $h$ , (b) at  $\text{H}_2\text{SO}_4$  concentration  $C_{a,0} = 5\%$  w/v, current densities  $j = 15$  and  $35 \text{ mA cm}^{-2}$  and in saturated  $\text{H}_2\text{SO}_4$  solution,  $C_{s,0} = C_{s,s}$ , and pure  $\text{H}_2\text{SO}_4$  solution,  $C_{s,0} = 0$



**Fig. 3** Variation of the dimensionless factor  $A$  with time,  $t$ , (a) and film thickness,  $h$ , (b) at  $\text{H}_2\text{SO}_4$  concentration  $C_{a,0} = 5\%$  w/v, current densities  $j = 15$  and  $35 \text{ mA cm}^{-2}$  and in saturated  $\text{H}_2\text{SO}_4$  solution,  $C_{s,0} = C_{s,s}$ , and pure  $\text{H}_2\text{SO}_4$  acid solution,  $C_{s,0} = 0$

plot profiles deviate strongly from that predicted by Eqs. 2 and 3 while the appearance of colloidal micelles is excluded. The other plots show growth of micelles; the Eq. 4 gave for  $C_{s,0}=C_{s,s}$   $A_0=0.3156$ ,  $A_1=-8 \times 10^{-4} \text{ min}^{-1}$  and  $A_2=9 \times 10^{-6} \text{ min}^{-2}$  at  $j=15 \text{ mA cm}^{-2}$  and  $A_0=0.2262$ ,  $A_1=-5 \times 10^{-4} \text{ min}^{-1}$  and  $A_2=2 \times 10^{-5} \text{ min}^{-2}$  at  $j=35 \text{ mA cm}^{-2}$ . At  $j=15 \text{ mA cm}^{-2}$  the  $A$  (or  $p$ ) for low  $h$ 's is higher at  $C_{s,0}=C_{s,s}$  than at  $C_{s,0}=0$  but beyond some  $h$  the trend is reversed. The span of  $A$  variation is smaller at  $C_{s,0}=C_{s,s}$  than at  $C_{s,0}=0$ .

As verified at  $j=15 \text{ mA cm}^{-2}$  and  $t=15 \text{ min}$ ,  $m$  decreased and  $A$  increased with  $C_{a,0}$  in both cases,  $C_{s,0}=0$  and  $C_{s,0}=C_{s,s}$ , while the  $m$  and  $A$  values at  $C_{s,0}=C_{s,s}$  were, respectively, lower and higher than those at  $C_{s,0}=0$ . Citation of numerical results has no significance, but these trends show that the  $A$  versus  $t$  plots at lower  $C_{a,0}$ 's may be qualitatively similar to those at  $C_{a,0}=5\% \text{ w/v}$  and shifted on average downwards as  $C_{a,0}$  decreases.

### Derivation of basic features of nanostructure

Since at  $j=15 \text{ mA cm}^{-2}$   $n=1.269 \times 10^{11} \text{ cm}^{-2}$  [12] and the ratio of  $n$ 's at  $j=15$  and  $35 \text{ mA cm}^{-2}$  is 1.31 [36], at the latter  $j$  the mean  $n \approx 9.687 \times 10^{10} \text{ cm}^{-2}$ . The average  $D_b=(A_0/n)^{1/2}$  for  $h \rightarrow 0$  is  $\approx 15.8$  and  $18.1 \text{ nm}$ , i.e. of nm scale. It is not notably affected by  $j$ ; the slight difference is attributed mainly to rise of temperature at pore bases that is enhanced with  $j$  (see later). Since  $nD_c^2=4/3$  [47], the mean  $D_c$  is  $\approx 32.4$  and  $37.1 \text{ nm}$ , respectively.

## Discussion

The overall processes and conditions inside the pores during the growth of film in low acidity baths

The phenomena inside the pores during Al anodising are complex, determining each other, and greatly affect the mechanism of film growth. For a satisfactory interpretation of results in low acidity baths, as here, the processes and conditions inside pores must be first discussed.

### Overall processes occurring inside the pores

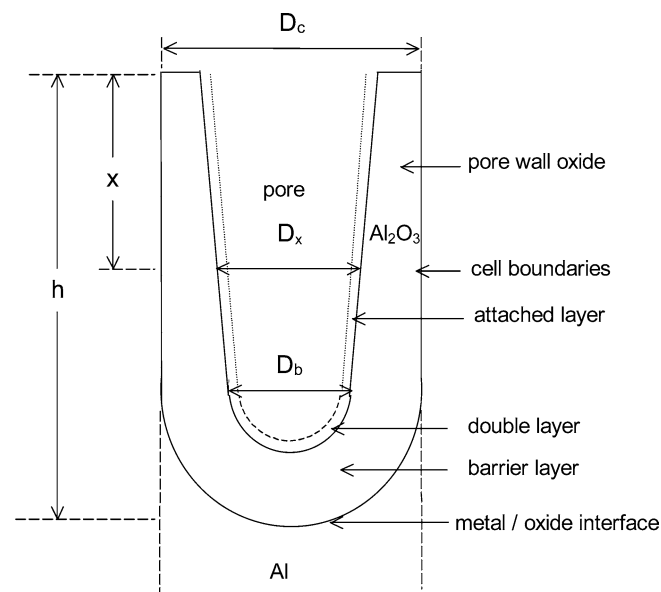
The oxide is formed in the oxide/Al interface, Fig. 4, according to Faraday's law [47, 51]. The Mass balance of anodic processes shows that  $\text{H}_2\text{O}$  is consumed yielding  $\text{O}^{2-}$  for oxide production in amounts corresponding to pore walls around pore bases and  $\text{H}^+$  ions released at pore bases [28, 52] ( $2\text{Al} + 3\text{H}_2\text{O} - 6e^- \rightarrow \text{Al}_2\text{O}_3 + 6\text{H}^+$ ).  $\text{Al}_2(\text{SO}_4)_3$  is formed by the "field assisted" pore base surface oxide dissolution [2, 3, 30, 32–34, 48–50], actually through the rejection and then hydration of  $\text{Al}^{3+}$  and migration of  $\text{O}^{2-}$  inwards barrier layer [28]. It is formed also by the chemical pore wall oxide

dissolution [2, 37–41] ( $\text{Al}_2\text{O}_3 + 3\text{H}_2\text{SO}_4 \rightarrow \text{Al}_2(\text{SO}_4)_3 + 3\text{H}_2\text{O}$ ). It enters the pore filling solution which, even at  $C_{s,0}=0$ , contains  $\text{Al}_2(\text{SO}_4)_3$ . The rate of oxide formation exceeds that of dissolution. The rate of  $\text{H}_2\text{O}$  consumption exceeds that of its production and  $\text{H}_2\text{O}$  (together with anions) rushes inwards the pores, filling them; this process occurs, up to the achievement of the maximum possible  $h$  or  $m$  [42, 43] at  $t \geq t_c$ , when it really occurs, where the rates of oxide production and dissolution become identical.

The heat evolved during Al anodising, mainly around pore bases, that increases with  $j$  and  $\Delta V$  is dissipated to the bath solution mainly through the pore filling solution, which has higher thermal conductivity than the oxide. A gradient of temperature is set up along the pores [42]. That around pore bases ( $T_b$ ) is higher than  $T$  and that at position  $x$ , Fig. 4, ( $T_x$ ) decreases towards the pore mouths. The  $T_x - T$  increases with  $x$ ,  $j$  and  $\Delta V$  and decreases with  $T$  and diameter at position  $x$  ( $D_x$ ) [42]. The  $C_{a,0}$  and  $C_{s,0}$  may secondarily affect  $T_b$  and  $T_x$ . After transient phenomena end, at each  $t$  and  $x$  a quasi-steady state is attained for mass, charge and heat transfer.

*Steady-state conditions inside the pores during regular and irregular film growth at low  $C_{a,0}$ 's and both  $C_{s,0}=C_{s,s}$  and  $C_{s,0}=0$*

As shown at  $C_{a,0} \geq 15\% \text{ w/v}$  and  $C_{s,0}=C_{s,s}$  supersaturation dominates inside pores during film growth,



**Fig. 4** Schematic representation of a section parallel to the pore axis of an elongated, columnar cell of a porous anodic alumina film. The pore, the pore base diameter  $D_b$ , the pore diameter at a position  $x$  along the pores  $D_x$ , the cell size  $D_c$ , the pore wall oxide and the hemispherical shell shaped barrier layer are distinguished. Also, the metal | oxide interface and the cell boundaries are shown. The pore generally broadens towards the film surface as a result of the pore wall chemical dissolution reaction by the electrolyte inside the pores during the film growth

which is enhanced towards the pore base and as  $j$  increases and  $T_x$  decreases [46]. The concentration of  $H_2SO_4$  varies slightly along the pores and that of  $Al_2(SO_4)_3$  increases towards the bases of pores. This is valid also in the present case since there is no conceived reason for the opposite. Also at each  $j$  and  $h$ , the average  $D_x$  is lower (see later),  $\Delta V$  is higher and thus  $T_b - T$  and  $T_x - T$  are larger than at higher  $C_{a,0}$ 's [46]. Supersaturation favours the growth of  $Al_2(SO_4)_3$  micelles on the surface of pores but the rise of  $T_b$  and  $T_x$  acts oppositely [35, 46].

The study of quasi-steady-state transport phenomena inside the pores during anodising of Al in  $H_2SO_4$  solution considering regular film growth and  $T_x = T$  [44, 52] showed that the dependence of acid and  $Al_2(SO_4)_3$  concentrations around pore bases ( $C_{a,b}$  and  $C_{s,b}$ ) and at position  $x$  along the pores, Fig. 4, ( $C_{a,x}$  and  $C_{s,x}$ ) on  $h$ ,  $x$ ,  $j$ ,  $T$  and  $C_{a,0}$  is generally very complex. In the region of low  $C_{a,0}$ 's and the  $T$  employed here, the study of transport phenomena [44] showed that at  $C_{a,0} = 1\%$  w/v and lower  $j$   $C_{a,x}$  decreases up to a few ten  $\mu m$  and then rises slightly with  $x$  while at  $C_{a,0} = 5\%$  w/v  $C_{a,x}$  decreases slightly up to the  $x$  or  $h = 150 \mu m$  examined. At the higher  $j$  and both  $C_{a,0}$ 's,  $C_{a,x}$  decreases slightly with  $x$  in a region of a few  $\mu m$  and then strongly rises. The  $C_{a,x} - C_{a,0}$  varies with  $j$  by a complex way depending on  $h$ ,  $C_{a,0}$  and  $T$ . The concentration and activity of  $H^+$  in the bath solution ( $C_{H^+,0}$ ,  $a_{H^+,0}$ ), at position  $x$  along the pores ( $C_{H^+,x}$ ,  $a_{H^+,x}$ ) and at pore bases ( $C_{H^+,b}$ ,  $a_{H^+,b}$ ) must follow  $C_{a,0}$ ,  $C_{a,x}$  and  $C_{a,b}$ . The  $C_{s,x}$  increases with  $x$  and  $j$ , decreases with  $T$  and imperceptibly changes with  $C_{a,0}$  [44].

At the employed  $T$  and low  $h$ 's, the  $C_{a,b} - C_{a,0}$  passes through a minimum at  $j \approx 15 \text{ mA cm}^{-2}$  for  $C_{a,0} = 1\%$  w/v and at  $j \approx 20 \text{ mA cm}^{-2}$  for  $C_{a,0} = 5\%$  w/v [44]. These are the critical  $j$ 's ( $j_c$ ) above which pitting appears, defined by  $(h \rightarrow 0) \partial C_{a,b} / \partial j = 0$  [44, 45] or  $\partial a_{H^+,b} / \partial j = 0$  [53]. For both  $C_{a,0}$ 's and the higher  $j$  employed, the growth of pitting is justified, as indeed observed. But inconsistencies appear for the lower  $j$  at  $C_{a,0} = 1\%$  w/v where just detected pitting could at most appear, while, actually, it is strong, and at  $C_{a,0} = 5\%$  w/v where it should not appear, but, really, slight pitting appears. They mark a peculiar behaviour rather than experimental errors or some effect of  $T_b$ . At each  $h$ ,  $T_x - T$  must be also notable due to the relatively high  $\Delta V$ 's.

In both cases  $C_{s,0} = 0$  and  $C_{s,0} = C_{s,s}$ , the pitted surface generally gradually enlarges, the rest shrinks and the average  $j$ 's are re-arranged in the two regions, initially fast and then slowly until a pseudo-steady state is attained. Also changes in the composition of pore filling solution and  $T_x$  and their distribution along the pores occur [44]. The differences in local  $h$ ,  $D_b$ , barrier layer thickness,  $T_b$  and distributions of electrolyte composition and  $T_x$  in pores, which vary with  $t$ , predict a chaotic, non-linear behaviour characterised by loops of effects of different parameters especially for strong pitting [44]. A strict analysis of conditions inside pores, as in regular growth [44, 45,

52], and interpretation of overall kinetic data is thus prohibited. A qualitative only description is possible in view of dependence of conditions in pores on  $j$ ,  $T$ ,  $h$ , etc. for regular growth. Thus, e.g.  $h$  and  $T_b$  are higher in pitted regions; but  $C_{a,x}$  and  $C_{s,x}$  may be lower or higher affected by the different local  $j$ ,  $T_x$  and  $h$ .

Interpretations of results and peculiar characteristics of film growth mechanism

*Interpretation of  $\Delta V$  versus  $t$  or  $h$  plots and their relative positions and of  $\Delta V$  variation with  $C_{a,0}$ ,  $C_{s,0}$  and  $j$*

Figure 1 shows that at  $C_{s,0} = C_{s,s}$  after the transient,  $\Delta V$  varies slightly with  $t$  up to a high  $t$  or  $h$  forming a plot plateau with a slight minimum and then rises. This behaviour differs from that at higher  $C_{a,0}$ 's, e.g. 15% w/v,  $C_{s,0} = C_{s,s}$  and  $j = 15 \text{ mA cm}^{-2}$  where after the initial transient,  $\Delta V$  notably rose in a large  $t$  range and later it rose strongly while at  $j = 35 \text{ mA cm}^{-2}$   $\Delta V$  rose strongly immediately after the transient [35]. The increase of  $C_{s,b}$  enhances the growth of micelles rising the fraction of occupied pore base surface. The increase of  $T_b$  acts oppositely [35]. Supersaturation in pores favours maximal growth of micelles at each  $h$ . The low acidity of bath results in low  $D_b$  and large thickness of barrier layer  $2^{-1}(D_c - D_b)$  which requires high  $\Delta V$  notably rising  $T_b$ . At each  $j$ ,  $D_b$  [36] increases and  $2^{-1}(D_c - D_b)$  decreases with  $T_b$  reducing  $\Delta V$ . Both  $T_b$  and  $C_{s,b}$  increase with  $h$ . The effect of rising  $T_b$  is initially larger than that of  $C_{s,b}$ ; later the trend is reversed. Thus,  $\Delta V$  decreases up to  $t(\Delta V_m)$  and then an accelerated increase is observed due mainly to the rise of the above surface fraction and decrease of  $D_b$  with  $h$  [35]. Micelles are not formed at  $C_{s,0} = 0$  and a plateau appears in  $\Delta V$  versus  $t$  plot for all  $t$ 's  $> t(\Delta V_m)$ , where  $\Delta V$  slightly decreases with  $t$  due to some rise of  $T_b$  slightly increasing  $D_b$  and reducing  $2^{-1}(D_c - D_b)$ .

The  $\Delta V$  generally decreased with  $C_{a,0}$  at both  $C_{s,0} = C_{s,s}$  and  $C_{s,0} = 0$ . The average  $n$  and  $D_c$  depend only on  $j$  [36] and are almost identical but the  $D_b$  increases with  $a_{H^+,b}$  [28] that follows  $C_{a,b}$  or  $C_{a,0}$ ;  $2^{-1}(D_c - D_b)$  decreases reducing  $\Delta V$  [28]. The higher  $\Delta V$  at  $C_{s,0} = 0$  than at  $C_{s,0} = C_{s,s}$  in plots plateau for identical  $j$ , Fig. 1, is explained by that the average  $D_b$  is lower, following  $a_{H^+,b}$  [28], while  $D_c$  is almost identical; thus,  $2^{-1}(D_c - D_b)$  is larger at  $C_{s,0} = 0$  requiring higher  $\Delta V$  [28], irrespective of any effect of micelles on  $\Delta V$  at  $C_{s,0} = C_{s,s}$ . Beyond the plateau, at  $C_{s,0} = C_{s,s}$  the surface fraction occupied by micelles increases,  $D_b$  decreases and  $\Delta V$  gradually exceeds that at  $C_{s,0} = 0$ . At  $C_{s,0} = C_{s,s}$  and each  $h$   $\Delta V$  increases with  $j$  since, irrespective of the effect of  $2^{-1}(D_c - D_b)$  value and double layer on  $\Delta V$ , the average field strength across the barrier layer and that surface fraction increase with  $j$  [28, 35].



*Real conditions inside the pores establishing a long initial transient stage at low  $C_{a,0}$ 's and  $C_{s,0}=0$ ; interpretation of the  $A$  versus  $t$  or  $h$  plots and of pitting appearance conditions*

At  $C_{s,0}=0$ ,  $j=15 \text{ mA cm}^{-2}$  and  $h \rightarrow 0$ ,  $nD_b^2 \approx 0.15$ , Fig. 3, and  $D_b \approx 10.9 \text{ nm}$ . The growth of film starts as regular and later it becomes irregular [44]. In the quasi-steady state, this  $j$  and  $T=25 \text{ }^\circ\text{C}$ , the equation [28]

$$(nD_b^2)^{-1} = 0.3947a_{\text{H}^+,\text{b}}^{-1} + 2.2645 \quad (5)$$

is valid for regular growth. For  $h \rightarrow 0$   $a_{\text{H}^+,\text{b}}$  is found 0.090 that is small enough compared to  $a_{\text{H}^+,\text{0}}=10^{-\text{pH}}=0.388$ . Such a drop of acidity is not predicted by the quasi-steady state transport analysis [44]. The conditions inside the pores in the first stage of strong increase of  $A$  with  $t$  deviate strongly from the quasi-steady state ones. This must be a long transient stage where the acidity at pore bases becomes low enough or  $\text{H}^+$  ions are almost depleted. The validity of this suggestion is tested below: In conditions close to steady state ones, pitting is just detectable and equation (2) must roughly apply. If the results beyond the long transient, i.e. for  $t > 30 \text{ min}$ , are considered, then  $A_0$  is  $\approx 0.29$ . Adopting that  $a_{\text{H}^+,\text{0}} \approx a_{\text{H}^+,\text{b}}$ , from Eq. 5  $nD_b^2 \approx 0.30$  that is close to 0.29; then the steady state  $D_b$  is  $\approx 15.4 \text{ nm}$ . If, as expected, the depletion of  $\text{H}^+$  is stronger on decreasing  $C_{a,0}$ , the transient region of the  $A$  versus  $t$  or  $h$  plots must become larger. Earlier  $A$  versus  $t$  plots results at  $C_{a,0}=2$  and 3% w/v [43] exactly confirmed it.

The double layer on the pore base surface consists of the fixed layer, containing mainly  $\text{SO}_4^{2-}$  [28] and the diffuse layer, containing all ions.  $\text{Al}^{3+}$  and  $\text{H}^+$  are rejected from that surface, traverse the fixed layer and drop in the diffuse layer where they become hydrated. The concentrations of cations and positive charge must increase towards the boundary of diffuse layer and pore filling solution where almost electroneutrality is first attained; the concentrations of  $\text{SO}_4^{2-}$  and  $\text{HSO}_4^-$  and negative charge accordingly decrease. The hydration number of  $\text{Al}^{3+}$  is high, 26 on average [54], consistent with the high hydration enthalpy. The diameter of hydrated ion group must be at least that of a sphere consisting of 26  $\text{H}_2\text{O}$  molecules, assuming that the small size of  $\text{Al}^{3+}$ , with radius  $\approx 0.057 \text{ nm}$  [54], is compensated by compressive attractive forces. From the molar volume of  $\text{H}_2\text{O}$ ,  $18 \text{ cm}^3 \text{ mol}^{-1}$ , the diameter of group is found  $> 1.1 \text{ nm}$  that is large compared to the non-equilibrium  $D_b$  when  $h \rightarrow 0$ . The hydration enthalpy and number of anions are low [54] and their size is close to that of unhydrated ions.

Beyond the diffuse layer, the current is conducted mainly by cations [55]. For  $h \rightarrow 0$  the flux rate of migrating  $\text{Al}^{3+}$  is low due to low concentration ( $\rightarrow 0$ ) and large size of hydrated  $\text{Al}^{3+}$  groups; as it approaches  $D_x$ , hindrances to their migration may be exerted either mutually or by the attached layer, Fig. 4. At low  $h$ 's

$\text{Al}^{3+}$  ions accumulate as  $h$  increases, thus increasing  $C_{s,x}$  and enhancing hindrances. The migration of  $\text{H}^+$  is easier, due to its hopping mechanism; the current is conducted almost solely by  $\text{H}^+$ . Though the rate of  $\text{H}^+$  production at pore bases is higher at lower  $D_b$  [46], the concentration of  $\text{H}^+$  is low and they are almost depleted, more at lower  $C_{a,0}$ .

The nucleation of pores may occur in small cracks created by mechanical stresses [28] and destined to become pores. The high acidity deters depletion of  $\text{H}^+$  and they are quickly transformed to pores, with  $D_b$  close to steady state one, and transient early ends. Low acidity allows almost depletion of  $\text{H}^+$  inside pores at low  $h$ 's. The  $D_b$  is small,  $2^{-1}(D_c - D_b)$  is large and  $\Delta V$  is high enough causing the rise of  $T_b$  and  $T_x$  with  $h$ , which result in the gradual increase of  $D_b$  and  $D_x$ . Also  $C_{s,b}$  must increase. At  $h > 0$  all these gradually increase the flux rate of migrating  $\text{Al}^{3+}$  and reduce  $\text{H}^+$  depletion. These processes continue until the pores widen enough and the transport phenomena,  $D_b$  and  $D_x$  approach the steady state ones. The transient ends when  $C_{\text{H}^+,\text{b}}$  or  $a_{\text{H}^+,\text{b}}$  approach  $C_{\text{H}^+,\text{0}}$  or  $a_{\text{H}^+,\text{0}}$  and distribution of all ions inside pores approaches that given by the steady-state transport analysis [44, 52].

In the quasi-steady state and at  $h$ 's comparable to the present ones, the  $C_{\text{H}^+,\text{x}}$  or  $a_{\text{H}^+,\text{x}}$  do not largely differ from  $C_{\text{H}^+,\text{0}}$  or  $a_{\text{H}^+,\text{0}}$  while as  $C_{\text{H}^+,\text{0}}$  or  $a_{\text{H}^+,\text{0}}$  decreases,  $j_c$  also decreases [44]. In the transient stage and for  $h \rightarrow 0$ , the  $C_{\text{H}^+,\text{b}}$  or  $a_{\text{H}^+,\text{b}}$  become much lower than  $C_{\text{H}^+,\text{0}}$  or  $a_{\text{H}^+,\text{0}}$  so that the real  $j_c$  decreases compared to the steady state one. This justifies the growth of pitting at  $j$ 's not predicted by the steady-state transport analysis. As  $h$  increases,  $C_{\text{H}^+,\text{b}}$  or  $a_{\text{H}^+,\text{b}}$  and  $j_c$  increase. Beyond some  $h$ ,  $j_c$  may become  $\geq j$ , the progress of pitting ends, regular film growth is set up and the pitted regions may be gradually repaired. That's why at  $C_{a,0}=5\%$  w/v pitting did not grow enough, but remained just detectable even up to  $t=160 \text{ min}$ . The transient in the  $\Delta V$  versus  $t$  or  $h$  plots must be also long at low  $C_{a,0}$ 's, as indeed shown in Fig. 1. But, the transient  $t$  range is shorter than that of  $A$  versus  $t$  or  $h$  plots. The first plots concern almost solely the processes in the region from double layer at pore bases to the oxide|metal interface, which may show shorter transients; the second plots concern, besides those, the processes of pore wall dissolution which may show longer transients. The characteristic  $A$  versus  $t$  or  $h$  plot profile at  $C_{s,0}=0$  is thus mainly due to the long transient and not to pitting development "per se" which must exert secondary effects.

*Interpretation of both the relative positions of  $A$  versus  $t$  or  $h$  plots at different conditions and the strongly different plot profiles at  $C_{s,0}=C_{s,s}$  and  $C_{s,0}=0$*

The higher  $A$ 's at  $C_{s,0}=C_{s,s}$  than at  $C_{s,0}=0$  for  $h \rightarrow 0$  are due mainly to the fact that, though  $D_c$  is comparable, the average  $D_b$  is larger in the first case owing to the higher  $a_{\text{H}^+,\text{b}}$  [28] that follows  $a_{\text{H}^+,\text{0}}$  while  $D_b$  in the second case is

further reduced due to the long transient stage that decreases  $a_{H+,b}$ . At  $h > 0$ , the  $D_b$  at  $C_{s,0} = C_{s,s}$  gradually decreases and later it becomes even lower than that at  $C_{s,0} = 0$  in the quasi-steady state for identical  $t$  or  $h$  due to the growth and effect of micelles which are enhanced with  $h$  [35]. The rate of wall dissolution at position  $x$  ( $r_x$ ) depends linearly on both the  $a_{H+,x}$  and free surface fraction not occupied by micelles [35]; it also decreases with the concentration of incorporated anions in the pore wall oxide which is much higher at  $C_{s,0} = C_{s,s}$  than at  $C_{s,0} = 0$  [28]. At  $C_{s,0} = C_{s,s}$  the higher  $a_{H+,x}$  increases  $r_x$  and the lower above fraction ( $< 1$ ) reduces it. The second effect and that of anions dominate so that the average  $r_x$  is lower at  $C_{s,0} = C_{s,s}$ . The average gradient of  $A$  versus  $t$  or  $h$  plots and the span of  $A$  variation are thus smaller at  $C_{s,0} = C_{s,s}$ . The plots at this  $C_{s,0}$  are shifted downwards with  $j$  due to decrease of  $n$  [36] and stronger growth of micelles and effect on  $D_b$  and average  $r_x$ .

The concentrations (and activities) of  $Al^{3+}$  and  $H^+$  are higher at  $C_{s,0} = C_{s,s}$  than at  $C_{s,0} = 0$ . The Eq. 5 and  $a_{H+,0} = 10^{-pH} = 0.906$  give for the lower  $j$ ,  $nD_b^2 \approx 0.37$  that is near  $A_0 \approx 0.32$  found by Eq. 4; the difference is due to the appearance of micelles which gradually reduce  $D_b$ , to some uncertainties owing to the scatter of points in the  $A$  versus  $t$  or  $h$  plots at  $C_{s,0} = C_{s,s}$ , etc. The  $A$  versus  $t$  or  $h$  plots at  $C_{s,0} = C_{s,s}$  do not show detectable transient. But at  $C_{s,0} = 0$  they include the initial long transient, where  $A$  strongly rises with  $t$  or  $h$ , and the quasi-steady state one. The strongly different  $A$  versus  $t$  or  $h$  plots profiles at  $C_{s,0} = 0$  and  $C_{s,0} = C_{s,s}$  are thus justified.

At the employed  $T$  and each  $j$ , the average  $A$  and the span of  $A$  variation here are smaller than those at  $C_{a,0} = 15\text{--}105\%$  w/v for comparable  $h$  ranges either at  $C_{s,0} = 0$  or  $C_{s,0} = C_{s,s}$  [43, 46]; this is due to the lower average  $D_b$  and  $r_x$  (and thus  $D_x$ ), resulted from the much lower  $C_{H+,b}$  or  $a_{H+,b}$  and  $C_{H+,x}$  or  $a_{H+,x}$ .

#### *Interpretation of development of salt deposit layer on the pitted regions of Al anode surface*

The deposition of salt on the P or B regions was never before observed at  $C_{a,0} = 15\text{--}105\%$  w/v,  $j = 15 \text{ mA cm}^{-2}$  and  $C_{s,0} = 0$  [43], as expected, while at  $C_{s,0} = C_{s,s}$  [46] it was occasionally met only at very high  $j$ 's  $\geq 105 \text{ mA cm}^{-2}$ . As shown here, it is not developed at  $C_{a,0} = 1\text{--}5\%$  and  $C_{s,0} = 0$ .  $Al_2(SO_4)_3$  precipitate is not formed inside the pores [35]. A considerable flux of  $Al^{3+}$  from pores to bath solution occurs due to conduction of current almost solely by cations [55] and increase of  $C_{s,x}$  with  $x$ . In the bath bulk solution the concentrations of  $Al^{3+}$  and  $SO_4^{2-}$  obey the solubility constant value and are higher while that of  $H_2O$  is lower than those at higher  $C_{a,0}$ 's and  $C_{s,0} = C_{s,s}$  [46]. The solution is viscous enough and an electrolyte layer is attached on the anode surface. The  $H_2O$  required to fill the pores comes from this layer. The concentration of  $H_2O$  inside it drops towards the pore mouths and the concentrations of  $Al^{3+}$  and  $SO_4^{2-}$  accordingly increase.

Supersaturation may appear in this layer similarly enlarged. The agitation occurring to some extent inside it may reduce the supersaturation. Salt precipitate appears starting from film surface. Its grains are relatively easily removed by the agitated solution.  $H_2SO_4$  feeds the salt deposition with anions and the cathodic reaction ( $2H_3O^+ + 2e \rightarrow 2H_2O + H_2$ ) with  $H^+$ .

The flux of  $Al^{3+}$  outwards and  $H_2O$  inwards the pores and deposition of salt in the non-pitted surface are slow and all particles of deposit are removed. But in the pitted regions these phenomena are fast, stirring is unable to remove all particles of deposit and some amount is attached on the surface; it increases with  $t$  and probably tends to a limit. Though at  $C_{a,0} = 5\%$  w/v and the higher  $j$  employed the deposit was clear, it was not at the lower  $j$  due to the small pitted surface, weak pitting, small enough rate of deposit formation and the removal of all its particles. The fact that at  $C_{s,0} = C_{s,s}$  and higher  $C_{a,0}$ 's deposit was observed only at much higher  $j$ 's [46], is then due to that only at such high  $j$ 's the concentrations of  $Al^{3+}$  and  $SO_4^{2-}$  become high and that of  $H_2O$  becomes low enough in the layer attached on anode surface so that the conditions resemble the above noted ones.

#### *Interpretation of peculiarities in pitting appearance conditions*

In  $H_2SO_4 + Al_2(SO_4)_3$  electrolytes with identical  $C_{a,0} \leq 15\%$  w/v and different  $C_{s,0}$ 's up to that at which micelles do not appear on pore base surface the steady state  $j_c$  decreases with  $C_{s,0}$  [35]. Then  $j_c$  strongly rises with  $C_{s,0}$ , due to the increase of amount of micelles per unit surface at pore bases that becomes highest at  $C_{s,0} = C_{s,s}$ . At  $C_{a,0} \geq 15\%$  w/v,  $C_{s,0} = C_{s,s}$  and each  $T, j_c$  exceeds that at  $C_{s,0} = 0$  [35, 46]. But at low  $C_{a,0}$ 's as here, the opposite is valid. This is rather due to effects of viscous solution on transport phenomena (more than at higher  $C_{a,0}$ 's), notable  $T_x - T_s$ , etc. at  $C_{s,0} = C_{s,s}$ , that reduce the control of film growth by micelles although  $T_b$  is larger rising  $j_c$ . Pitting is thus stronger at  $C_{s,0} = C_{s,s}$  than at  $C_{s,0} = 0$  where as noted it is ascribed mainly to the initial transient.

For  $C_{a,0} = 5\%$  w/v and  $C_{s,0} = C_{s,s}$  the steady state and real  $j_c$ 's coincide and as  $j$  decreases pitting weakens. At  $j = 15 \text{ mA cm}^{-2}$  pitting is just detected; thus this  $j$  just exceeds  $j_c$ . The difference of steady state  $j_c$ 's at  $C_{s,0} = C_{s,s}$  and  $C_{s,0} = 0$  shrinks with  $C_{a,0}$ , since the previous effective factors weaken. At a  $C_{a,0}$ ', just exceeding  $5\%$  w/v, they coincide. At  $C_{a,0} < C_{a,0}'$  and each  $j$  pitting is stronger, or the steady state  $j_c$  is lower, at  $C_{s,0} = C_{s,s}$  but at  $C_{a,0} > C_{a,0}'$  the trends are reversed, conforming to those at  $C_{a,0} \geq 15\%$  w/v [46].

The possibility to optimise the regular film growth in low acidity sulphate baths

The non use of low acidity  $H_2SO_4$  baths in practice to produce low  $p$  hard films is due thus to the long transient,

accompanied by the growth of abnormally strong pitting and high  $\Delta V$ 's. The use of saturated baths cancels that long transient. The effect of micelles and incorporated anions gradually dominate over that of their higher acidity at  $h \gg 0$  and  $p$  becomes lower even than that at  $C_{s,0} = 0$ . But the steady state  $j_c$  may be still higher.

Al anodising at low  $C_{a,0}$ 's and  $C_{s,0} = C_{s,s}$  shows many peculiarities when compared to that at similar  $C_{a,0}$ 's and  $C_{s,0} = 0$  and at  $C_{a,0} \geq 15\%$  w/v and  $C_{s,0} = C_{s,s}$  [35, 46]. During regular film growth, e.g. at  $j < 15 \text{ mA cm}^{-2}$ , a behaviour like that in Fig. 3 is expected. The growth of films at high  $h$ 's with  $p$  lower or at low  $h$ 's with  $p$  higher than that at similar  $C_{a,0}$ 's and  $C_{s,0} = 0$  is thus possible. Also films with  $p$  lower than that at  $C_{s,0} = C_{s,s}$  and higher  $C_{a,0}$ 's, e.g.  $C_{a,0} = 15\text{--}105\%$  w/v [46], can be formed. At these  $j$ 's they will have high  $n$  and  $p$  lower than that at  $C_{s,0} = 0$  and high  $h$ 's and at higher  $C_{a,0}$ 's and almost all  $h$ 's. Much higher  $h$ 's than in other cases, and irrespective of  $D_b$ , much higher maximum limiting  $h$ 's and real surfaces needed in applications like adsorption, catalysis, etc. thus can be achieved. These constitute an optimisation of process that can be further extended by varying  $T$  [46].

## Conclusions

- Anodising of Al was performed galvanostatically at constant  $T$  in solutions of  $\text{H}_2\text{SO}_4$ , 0–5% w/v, pure and saturated by  $\text{Al}_2(\text{SO}_4)_3$  and studied by chronopotentiometry and overall kinetics. It took place even in pure  $\text{Al}_2(\text{SO}_4)_3$  solution, which was acidic enough. Al anodising in low acidity solutions saturated and pure shows many peculiarities either when these baths or these with higher acidity baths are compared, like differences of porosity and its dependence on film thickness, lower critical current densities above which pitting appears in saturated than in pure acid solutions, salt deposition on pitted surfaces in the first, etc.
- The different conditions in pores are responsible for these peculiarities. Such differences are supersaturation and higher temperature, due to the needed higher anodic potential, and more viscous solution in saturated baths of low acid concentrations than at high ones, almost depletion of  $\text{H}^+$  during a long initial transient stage in similar low concentrations pure acid baths, etc. Saturated low acid concentration baths cancel this transient and prevail as regards the mechanism of growth and structure of low porosity films at specific conditions.
- Pitting always appeared at the  $j$ 's employed; it was stronger in saturated than in pure acid solutions and weakened with acid concentration. A threshold  $C'_{a,0}$  exists, just exceeding 5% w/v, where the steady-state critical current density  $j_c$  is identical for both pure and saturated solutions. At  $C_{a,0} < C'_{a,0}$  it is lower for saturated ones but at  $C_{a,0} > C'_{a,0}$  the trend is reversed

resembling that at  $C_{a,0} \geq 15\%$  w/v [46]. Optimisation of regular film growth is possible in these baths at  $j$ 's  $< j_c$ 's as regards certain structural features, as at higher  $C_{a,0}$ 's.

- The present and earlier [35, 46] results, allow the optimisation of conditions to produce regularly grown, uniform, high quality films of desired/designed structure and  $p$  varying in large ranges and essentially introduce new technologies. Yet unsolved problems may be solved like the production of regular films with desired low porosity for mechanical applications and protection technologies and high pore surface density, probably pore base diameter, thickness and real surface for applications involving reactivity of material like adsorption, catalysis, etc. Also, they may be used in more recent applications like nanoscience/nanotechnology, etc.

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